

More problems for section 3.4 of *Essentials of Precalculus with Calculus Previews* by Zill and Dewar, 5e.

1. Find all zeros and factor completely.

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| a. $x^3 - x^2 - 10x - 8$ | b. $4x^3 + 8x^2 - 15x - 9$ | c. $25x^3 - 85x^2 - 58x - 8$ |
| d. $3x^3 - 18x^2 + 15x + 36$ | e. $4x^3 - 4x^2 - x + 1$ | f. $3x^3 + 7x^2 - 22x - 8$ |
| g. $5x^4 + 16x^3 - 17x^2 - 64x - 12$ | h. $x^4 + 6x^3 + x^2 - 24x - 20$ | i. $x^4 - 5x^3 - 19x^2 + 29x + 42$ |
| j. $3x^4 - 8x^3 - 15x^2 + 32x + 12$ | k. $x^4 - 2x^3 - 7x^2 + 20x - 12$ | l. $x^4 + 5x^3 + x^2 - 21x - 18$ |
| m. $x^4 - 4x^3 - 3x^2 + 10x + 8$ | n. $x^4 + x^3 - 12x^2 + 4x + 16$ | o. $x^3 + 5x^2 + 5x - 2$ |
| p. $2x^3 - 4x^2 - 7x + 3$ | q. $2x^3 + 5x^2 - 7x + 2$ | r. $3x^3 + 4x^2 - 14x - 5$ |
| s. $x^4 + 3x^3 - 11x^2 - 23x + 6$ | t. $x^4 - 9x^2 + 14$ | u. $x^4 - 12x^2 + 27$ |
| v. $x^4 + 5x^3 - 4x^2 - 20x$ | w. $2x^4 + 5x^3 - 18x^2 - 26x - 8$ | x. $3x^4 + 10x^3 - 30x^2 + 10x + 7$ |
| y. $3x^3 + 4x^2 - 14x - 5$ | | |

2. Find all zeros and factor completely.

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|---------------------------------|---------------------------------|------------------------------------|
| a. $x^2 + 4$ | b. $x^2 - 2x + 5$ | c. $x^2 + 4x + 7$ |
| d. $x^4 + x^3 + x^2 + 3x - 6$ | e. $2x^4 - x^3 + 7x^2 - 4x - 4$ | f. $3x^4 + 7x^3 - 7x^2 - 33x - 10$ |
| g. $2x^4 - 13x^2 - 13x - 6$ | h. $x^4 + 5x^2 + 4$ | i. $x^4 + 2x^2 - 15$ |
| j. $x^4 + 2x^3 + x^2 - 8x - 20$ | k. $x^4 - 15x^2 - 44x - 30$ | l. $x^4 - 81$ |

Answers

- 1a. $(x+1)(x+2)(x-4); x = -1, -2, 4$. 1b. $(2x+1)(2x-3)(x+3); x = -1/2, 3/2, -3$. 1c. $(5x+1)(5x+2)(x-4); x = -1/5, -2/5, 4$.
1d. (factor out 3) $3(x+1)(x-3)(x-4); x = -1, 3, 4$. 1e. $(x-1)(2x+1)(2x-1); x = 1, \pm 1/2$. 1f. $(3x+1)(x-2)(x+4); x = -1/3, 2, -4$.
1g. $(5x+1)(x+3)(x-2)(x+2); x = -1/5, -3, \pm 2$. 1h. $(x+1)(x+5)(x-2)(x+2); x = -1, -5, \pm 2$. 1i. $(x+1)(x+3)(x-2)(x-7); x = -1, -3, 2, 7$.
1j. $(3x+1)(x-3)(x-2)(x+2); x = -1/3, 3, \pm 2$. 1k. $(x-1)(x-2)^2(x+3); x = 1, 2, -3$. 1l. $(x+1)(x-2)(x+3)^2; x = -1, 2, -3$.
1m. $(x+1)^2(x-2)(x-4); x = -1, 2, 4$. 1n. $(x+1)(x-2)^2(x+4); x = -1, 2, -4$. 1o. $(x+2)(x - \frac{-3+\sqrt{13}}{2})(x - \frac{-3-\sqrt{13}}{2}); x = -2, (-3 \pm \sqrt{13})/2$.
1p. $(x-3)(x - \frac{-1+\sqrt{3}}{2})(x - \frac{-1-\sqrt{3}}{2}); x = 3, (-1 \pm \sqrt{3})/2$. 1q. $(2x-1)(x - \frac{-3+\sqrt{17}}{2})(x - \frac{-3-\sqrt{17}}{2}); x = 1/2, (-3 \pm \sqrt{17})/2$.
1r. $(3x+1)(x + (1 - \sqrt{21})/2)(x + (1 + \sqrt{21})/2); x = -1/3, (-1 \pm \sqrt{21})/2$. 1s. $(x+2)(x-3)(x+2-\sqrt{5})(x+2+\sqrt{5}); x = -2, 3, -2 \pm \sqrt{5}$.
1t. $(x-\sqrt{2})(x+\sqrt{2})(x-\sqrt{7})(x+\sqrt{7}); x = \pm\sqrt{2}, \pm\sqrt{7}$. 1u. $(x-3)(x+3)(x-\sqrt{3})(x+\sqrt{3}); x = \pm\sqrt{3}, \pm 3$.
1v. $x(x-2)(x+2)(x+5); x = 0, \pm 2, -5$. 1w. $(2x+1)(x+4)(x-1-\sqrt{3})(x-1+\sqrt{3}); x = -1/2, -4, 1 \pm \sqrt{3}$.
1x. $(3x+1)(x-1)(x+2-\sqrt{11})(x+2+\sqrt{11}); x = -1/3, 1, -2 \pm \sqrt{11}$. 1y. $(3x+1)(x + \frac{1+\sqrt{21}}{2})(x + \frac{1-\sqrt{21}}{2}); x = -1/3, (-1 \pm \sqrt{21})/2$.
2a. $(x-2i)(x+2i); x = \pm 2i$. 2b. $(x-1-2i)(x-1+2i); x = 1 \pm 2i$. 2c. $(x+2-i\sqrt{3})(x+2+i\sqrt{3}); x = -2 \pm i\sqrt{3}$. 2d. $(x-1)(x+2)(x+i\sqrt{3})(x-i\sqrt{3}); x = 1, -2, \pm i\sqrt{3}$.
2e. $(x-1)(2x+1)(x-2i)(x+2i); x = 1, -1/2, \pm 2i$. 2f. $(x-2)(3x+1)(x+2-i)(x+2+i); x = 2, -1/3, -2 \pm i$.
2g. $2(x+2)(x-3)(x+(1-i)/2)(x+(1+i)/2); x = -2, 3, (-1 \pm i)/2$. 2h. $(x-i)(x+i)(x-2i)(x+2i); x = \pm i, \pm 2i$.
2i. $(x-\sqrt{3})(x+\sqrt{3})(x-i\sqrt{5})(x+i\sqrt{5}); x = \pm\sqrt{3}, \pm i\sqrt{5}$. 2j. $(x+2)(x-2)(x+1-2i)(x+1+2i); x = \pm 2, -1 \pm 2i$.
2k. $(x+1)(x-5)(x+2+i\sqrt{2})(x+2-i\sqrt{2}); x = 5, -1, -2 \pm i\sqrt{2}$. 2l. $(x-3)(x+3)(x-3i)(x+3i); x = \pm 3, \pm 3i$